

Radical Equations

10th Grade

Squaring both sides solves it — and can invent answers that do not work.

Isolate the radical, square, solve — then check every answer in the original equation.

1 ISOLATE THE RADICAL

1

Get the root term alone on one side first.

2 SQUARE BOTH SIDES

2

This removes the root but may introduce false solutions.

3 SOLVE

3

Often a linear or quadratic equation.

4 CHECK EVERY ANSWER

4

Substitute into the ORIGINAL. Discard any that fail.

WHY CHECKING MATTERS

$$\sqrt{x+6} = x \rightarrow x + 6 = x^2 \rightarrow x = 3 \text{ or } -2$$

Check: $x = 3$ works. $x = -2$ gives $\sqrt{4} = -2$, which is false.

So $x = 3$ only.

Squaring is not reversible. That is exactly why extraneous solutions appear.